

**Practice 9-4****Example Exercises****Example 1**

Simplify each radical expression. Assume that all variables under radicals represent positive numbers.

1.  $\sqrt{50}$   

$$\frac{25 \cdot 2}{5 \cdot 2} = \frac{25}{5} \cdot \sqrt{2} = 5\sqrt{2}$$

2.  $\sqrt{48}$

7.  $\sqrt{300}$   

$$\frac{100 \cdot 3}{10 \cdot 3} = \frac{100}{10} \cdot \sqrt{3} = 10\sqrt{3}$$

8.  $\sqrt{49a^3}$

3.  $\sqrt{20}$   

$$\frac{4 \cdot 5}{2 \cdot 5} = \frac{4}{2} \cdot \sqrt{5} = 2\sqrt{5}$$

4.  $\sqrt{8}$

9.  $\sqrt{125}$   

$$\frac{25 \cdot 5}{5 \cdot 5} = \frac{25}{5} \cdot \sqrt{5} = 5\sqrt{5}$$

10.  $\sqrt{28}$

5.  $\sqrt{25x^4}$   

$$\frac{25x^4}{5x^2} = 5x^2 \cdot \sqrt{x^2} = 5x^2 \cdot x = 5x^3$$

6.  $\sqrt{75}$

11.  $\sqrt{63}$   

$$\frac{9 \cdot 7}{3 \cdot 7} = \frac{9}{3} \cdot \sqrt{7} = 3\sqrt{7}$$

12.  $\sqrt{72}$

**Example 2**

Simplify each radical expression. Assume that all variables under radicals represent positive numbers.

13.  $6\sqrt{20}$   

$$\frac{6 \cdot 4 \cdot 5}{6 \cdot 4} = 6 \cdot \sqrt{5}$$

14.  $\sqrt{8} \cdot \sqrt{2}$

18.  $(2\sqrt{3})^2$   

$$4(3) = 12$$

19.  $\sqrt{12} \cdot \sqrt{27}$

20.  $(7\sqrt{5})^2$   

$$49(5) = 245$$

21.  $\sqrt{a^5b^6}$

15.  $\sqrt{ab^3} \cdot b\sqrt{ab}$   

$$\frac{a \cdot b^3 \cdot b}{b \cdot b} = ab^2 \cdot \sqrt{ab}$$

22.  $\sqrt{30} \cdot \sqrt{6}$

16.  $\sqrt{12} \cdot \sqrt{60x^2}$   

$$12\sqrt{15x^2}$$

17.  $12\sqrt{60x^2}$   

$$12\sqrt{4 \cdot 15 \cdot x^2}$$

18.  $24\sqrt{15}$   

$$24\sqrt{4 \cdot 15} = 12\sqrt{15}$$

19.  $12\sqrt{15}$   

$$12\sqrt{4 \cdot 15} = 12\sqrt{4} \cdot \sqrt{15} = 24\sqrt{15}$$

20.  $12\sqrt{15}$   

$$12\sqrt{4 \cdot 15} = 12\sqrt{4} \cdot \sqrt{15} = 24\sqrt{15}$$

21.  $12\sqrt{15}$   

$$12\sqrt{4 \cdot 15} = 12\sqrt{4} \cdot \sqrt{15} = 24\sqrt{15}$$

22.  $12\sqrt{15}$   

$$12\sqrt{4 \cdot 15} = 12\sqrt{4} \cdot \sqrt{15} = 24\sqrt{15}$$

23.  $12$   
 $g$   
 $6$

24.  $4$   
 $g$   
 $2\sqrt{2}$

25.  $10$   
 $4\sqrt{6}$

**Examples 4-6**

Simplify each radical expression. Assume that all variables under radicals represent positive numbers.

26.  $\sqrt{\frac{7}{9}}$

27.  $\sqrt{\frac{17}{64}}$

$$\frac{\sqrt{17}}{\sqrt{64}} = \frac{\sqrt{17}}{8}$$

28.  $\frac{\sqrt{48}}{\sqrt{8}}$

29.  $\frac{\sqrt{120}}{\sqrt{10}}$

30.  $\frac{5}{\sqrt{2}}$

31.  $\frac{7}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}}$

32.  $\sqrt{\frac{15}{49}}$

$$\frac{\sqrt{15}}{\sqrt{49}} = \frac{\sqrt{15}}{7}$$

33.  $\frac{\sqrt{60}}{\sqrt{12}}$

34.  $\frac{3}{\sqrt{3}} \cdot \frac{\sqrt{3}}{\sqrt{3}}$

35.  $\frac{4}{\sqrt{8}}$

$$\frac{\sqrt{7 \cdot 3}}{\sqrt{3}} = \frac{\sqrt{21}}{\sqrt{3}} = \sqrt{7}$$

$$\sqrt{\frac{15}{49}} = \frac{\sqrt{15}}{\sqrt{49}} = \frac{\sqrt{15}}{7}$$

$$\frac{\sqrt{3} \cdot \sqrt{3}}{\sqrt{3}} = \frac{3}{\sqrt{3}} = \sqrt{3}$$

$$\frac{4}{\sqrt{8}} = \frac{4}{\sqrt{4 \cdot 2}} = \frac{4}{2\sqrt{2}} = \frac{2}{\sqrt{2}}$$

OR

$$\frac{4}{\sqrt{8}} = \frac{4}{\sqrt{4 \cdot 2}} = \frac{4}{2\sqrt{2}}$$

$$\frac{4}{2\sqrt{2}} = \frac{2}{\sqrt{2}}$$

$$\frac{2}{\sqrt{2}} = \sqrt{2}$$

$$\frac{\sqrt{2}}{\sqrt{2}} = 1$$

**Practice 9-5****Example Exercises****Example 1**

Simplify each expression.

1.  $5\sqrt{2} + 3\sqrt{2}$

2.  $8\sqrt{5} + 6\sqrt{5}$

14 $\sqrt{5}$

4.  $4\sqrt{7} + 3\sqrt{7}$

5.  $8\sqrt{10} + \sqrt{10}$

9 $\sqrt{10}$

7.  $10\sqrt{6} - 8\sqrt{6}$

8.  $2\sqrt{11} - 6\sqrt{11}$

-4 $\sqrt{11}$

3.  $\sqrt{6} + 2\sqrt{6}$

6.  $7\sqrt{3} - 2\sqrt{3}$

5 $\sqrt{3}$

9.  $-8\sqrt{15} + 10\sqrt{15}$

2 $\sqrt{15}$

**Example 2**

Simplify each expression.

10.  $3\sqrt{2} + \sqrt{8}$

11.  $\sqrt{27} + 4\sqrt{3}$

7 $\sqrt{3}$

13.  $\sqrt{28} + 6\sqrt{7}$

14.  $5\sqrt{3} - \sqrt{12}$

9 $\sqrt{5} - 2\sqrt{3}$

16.  $6\sqrt{2} - \sqrt{32}$

17.  $9\sqrt{5} - \sqrt{20}$

7 $\sqrt{5}$

19.  $\sqrt{32} - \sqrt{8}$

20.  $4\sqrt{3} - \sqrt{12}$

4 $\sqrt{2} - 2\sqrt{3}$

**Example 3**Solve each exercise by using the golden ratio  $(1 + \sqrt{5}) : 2$ .

- ~~22.~~ The ratio of the width : height of a door is equal to the golden ratio.  
The height of the door is 60 in. Find the width of the door in inches.

- ~~23.~~ The ratio of the length : width of a pool is equal to the golden ratio.  
The width is 30 ft. Find the length of the pool in feet.

**Example 4**

Simplify each expression.

24.  $3(4 + 2\sqrt{5})$

25.  $-2(6\sqrt{2} - 8)$

-12 $\sqrt{2} + 16$

15 $\sqrt{5} + 20\sqrt{3}$

27.  $\sqrt{3}(6 + 2\sqrt{2})$

28.  $\sqrt{5}(8 - 3\sqrt{5})$

2 $\sqrt{3}(1 + 8\sqrt{2})$

30.  $\sqrt{6}(\sqrt{2} - 6)$

31.  $\sqrt{3}(4\sqrt{5} - 6\sqrt{3})$

5(3 $\sqrt{2} + 4\sqrt{3})$

33.  $\frac{-6 \pm \sqrt{96}}{-6}$

34.  $\frac{15 \pm \sqrt{375}}{10}$

2 $\sqrt{3} + 16\sqrt{6}$

$$\frac{-6 \pm \sqrt{416}}{-6} = \frac{-3 \pm 2\sqrt{16}}{-3}$$

35.  $\frac{10}{15 \pm 5\sqrt{15}}$

15 $\pm \sqrt{15}$

$$\frac{-6 \pm \sqrt{416}}{-6} = \frac{-3 \pm 2\sqrt{16}}{-3}$$

36.  $\frac{3 \pm \sqrt{15}}{2}$

3 $\pm \sqrt{15}$