

Algebra I
Unit 7 Review

Name: Key

U7L1-3

1. What are the three methods we've learned for solving equations?

a. Square Roots (L1)

b. Factoring (L2)

c. Quadratic Formula (L3)

U7L1: Solve using square roots

2. $x^2 - 36 = 0$

$$\begin{array}{|c|} \hline x^2 = 36 \\ \hline x = \pm 6 \\ \hline \end{array}$$

3. $-20x^2 = -245$

$$\begin{array}{|c|} \hline x^2 = \frac{49}{4} \\ \hline x = \pm \frac{7}{2} \\ \hline \end{array}$$

U7L2: Solve by factoring

4. What is the zero product property? If $ab=0$, $a=0$ or $b=0$

5. $8t^2 - 32t = 0$

$$\begin{array}{|c|} \hline t = 0, 4 \\ \hline \end{array}$$

6. $4s^2 = 221 - 8s$

$$4s^2 + 8s - 221 = 0$$

$$4s^2 + 34s + -216s - 221 = 0$$

$$2(as + 17) - 13(as + 17) = 0$$

$$(as + 17)(as - 13) = 0$$

$$\begin{array}{|c|} \hline s = -\frac{17}{2}, \frac{13}{2} \\ \hline \end{array}$$

U7L3: Solve using the Quadratic Formula

7. What is the Quadratic Formula?

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

8. What is the discriminant? What does this tell us about our quadratic equation? WHY does it tell us this information?

$b^2 - 4ac$ # solutions under $\sqrt{}$

9. What is the U.S. equation for falling objects or projectiles? Describe what each variable represents in these equations.

$$h(t) = -16t^2 + v_0 t + h_0$$

↓ ↓ ↓
 height time initial
 initial velocity

10. $2y^2 = 39y - 17$ (answers can be decimals)

$$2y^2 - 39y + 17 = 0$$

$$x = \frac{-(-39) \pm \sqrt{(-39)^2 - 4(2)(17)}}{2(2)}$$

$$= \frac{39 \pm \sqrt{1385}}{4} \approx \frac{39 \pm 37.22}{4}$$

11. $8x^2 + 8x + 1 = 0$ (write EXACT answers; use radicals)

$$x = \frac{-8 \pm \sqrt{(8)^2 - 4(8)(1)}}{2(8)}$$

$$= \frac{-8 \pm \sqrt{32}}{16}$$

$$= \frac{-8 \pm 4\sqrt{2}}{16} = \boxed{-\frac{2 \pm \sqrt{2}}{4}}$$

$$\boxed{x \approx 19.06, \\ 0.45}$$

12. A ball is thrown upwards from a height of 15 feet with an initial velocity of 5 ft/s. Write an equation using height of a projectile formula. How long it will take for the ball to hit the ground?

$$h(t) = -16t^2 + 5t + 15$$

$$0 = -16t^2 + 5t + 15$$

$$\boxed{1.14 \text{ sec}}$$

$$x = \frac{-5 \pm \sqrt{5^2 - 4(-16)(15)}}{2(-16)}$$

$$= \frac{-5 \pm \sqrt{985}}{-32} \approx \frac{-5 \pm 31.38}{-32}$$

13. Use the discriminant to determine if the ball from the previous problem will ever reach a height of 32 feet.

$$5^2 - 4(-16)(-17)$$

$$-1063 < 0 \quad \boxed{\text{no}}$$

$$32 = -16t^2 + 5t + 15$$

$$0 = -16t^2 + 5t - 17$$

$$x \approx -0.82, \\ 1.14$$

U7L1-3:

- Find the discriminant
- Tell the number and type of solutions
- Choose the correct method to solve the equation (if there are any solutions)
- Find the solutions (if there are any) (write all solutions EXACT; use radicals if needed)

14. $54x^2 - 96 = 0$

a. $0^2 - 4(54)(-96)$
 $\boxed{20736}$

b. 2 rational sol

c. Square roots

d. $54x^2 = 96$

$$x^2 = \frac{16}{9}$$

$\boxed{x = \pm \frac{4}{3}}$

15. $6x^2 = 7x + 20$ $6x^2 - 7x - 20 = 0$

a. $(-7)^2 - 4(6)(-20)$

$\boxed{529}$

b. 2 rational sol

c. Factoring

d. $6x^2 - 7x - 20 = 0$

$$3x(2x - 5) + 4(2x + 5) = 0$$

$$(2x - 5)(3x + 4) = 0$$

$\boxed{x = \frac{5}{2}, -\frac{4}{3}}$

16. $-x^2 = 18 - 12x$ $0 = x^2 - 12x + 18$

a. $(-12)^2 - 4(1)(18)$
 $\boxed{72}$

b. 2 irrational sol

c. Quadratic Formula

d. $x = \frac{-(-12) \pm \sqrt{72}}{2(1)}$

$$= \frac{12 \pm \sqrt{72}}{2}$$

$= \boxed{6 \pm 3\sqrt{2}}$

17. $4x^2 + 81 = 0$

1. $0^2 - 4(4)(81)$

$\boxed{-1296}$

2. no sol

3.



4.

U7L4-5: Simplify each radical as much as possible

18. $\sqrt{448}$

$\boxed{8\sqrt{7}}$

24. $(10\sqrt{6})^2$

$\boxed{100(6)}$

$\boxed{600}$

19. $\sqrt{147}$

$\boxed{7\sqrt{3}}$

25. $\sqrt{\frac{17}{144}}$

$\boxed{\frac{\sqrt{17}}{12}}$

20. $\sqrt{80x^8}$

$\boxed{4x^4\sqrt{5}}$

26. $\frac{\sqrt{256}}{\sqrt{32}}$

$\boxed{\sqrt{8}}$

21. $\sqrt{256v^{11}}$

$\boxed{16v^5\sqrt{v}}$

27. $\frac{5}{\sqrt{7}} \cdot \frac{\sqrt{5}}{\sqrt{5}}$

$\boxed{\frac{5\sqrt{5}}{7}}$

22. $3\sqrt{24x^2y^5}$

$3 \cdot 2xy^2\sqrt{6}y$

$\boxed{6xy^2\sqrt{6}y}$

28. $\frac{4}{\sqrt{2a}} \cdot \frac{\sqrt{2a}}{\sqrt{2a}}$

$\frac{4\sqrt{2a}}{2a} = \boxed{\frac{2\sqrt{2a}}{a}}$

23. $\sqrt{15} \cdot \sqrt{35}$

$\boxed{\sqrt{525}}$

$\boxed{5\sqrt{21}}$

29. $\sqrt{\frac{12}{225}} = \frac{\sqrt{12}}{\sqrt{225}}$

$= \boxed{\frac{2\sqrt{3}}{15}}$

$$30. 10\sqrt{4} - \sqrt{4}$$

$$\boxed{9\sqrt{4}}$$

$$31. \sqrt{448} - 3\sqrt{432} + \sqrt{175}$$

$$8\sqrt{7} - 36\sqrt{3} + 5\sqrt{7}$$

$$\boxed{13\sqrt{7} - 36\sqrt{3}}$$

$$32. 3(8\sqrt{3} - 7)$$

$$\boxed{24\sqrt{3} - 21}$$

$$33. \sqrt{10}(3 - 2\sqrt{6})$$

$$3\sqrt{10} - 2\sqrt{60}$$

$$\boxed{3\sqrt{10} - 4\sqrt{15}}$$

$$34. 3\sqrt{6}(2\sqrt{3} + \sqrt{6})$$

$$6\sqrt{18} + 3(6)$$

$$\boxed{18\sqrt{2} + 18}$$